

# Quantum Information using Optical Superlattices

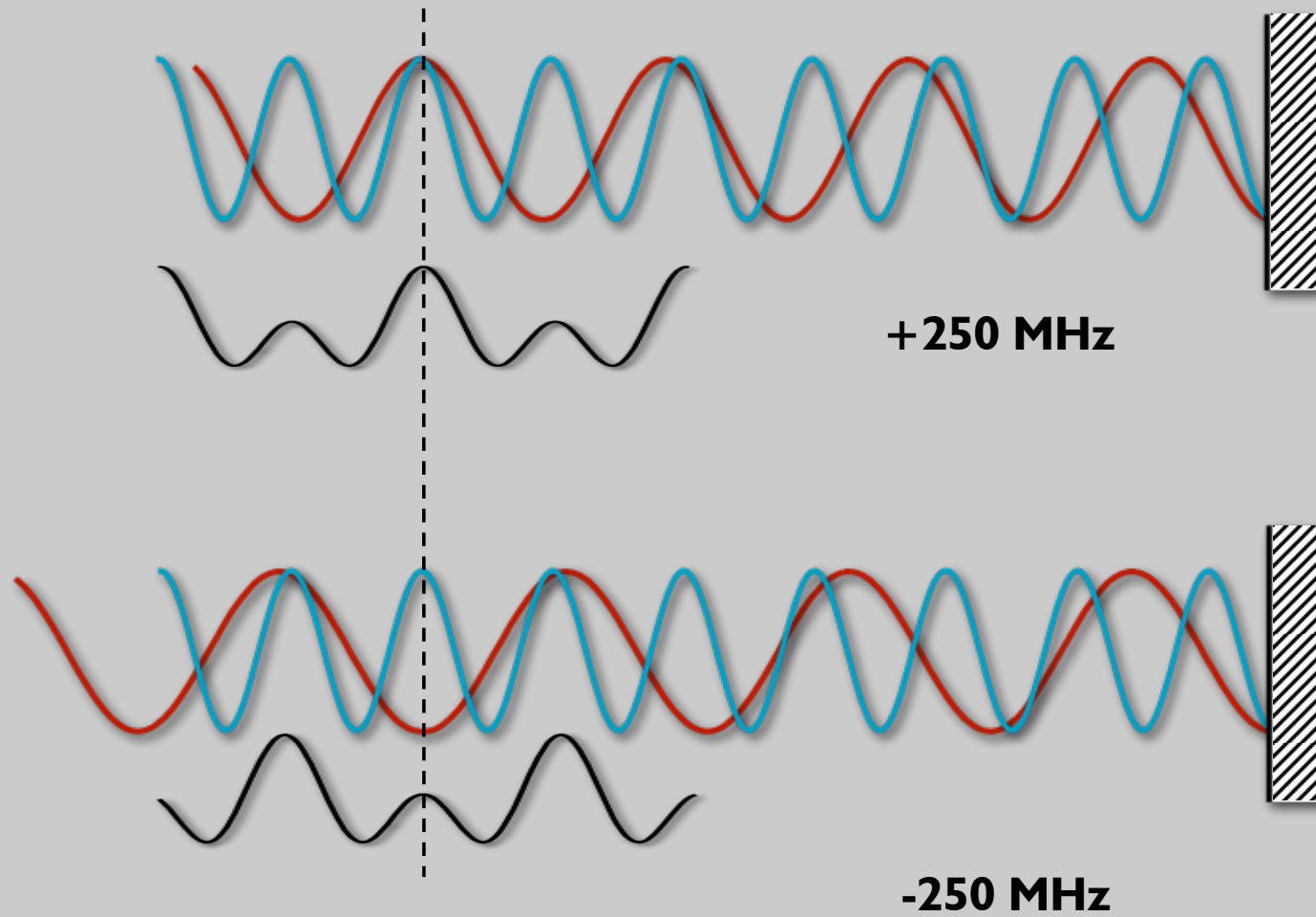


WP2,WP3,WP4,WP5

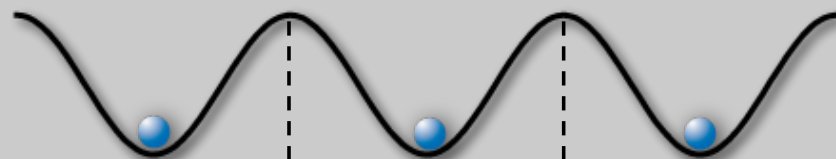
OLAQUI Review Meeting,  
Innsbruck

- **WP2 Addressing, manipulating and measuring on single sites**  
D5 Addressing single sites in optical lattices, M2.2
- **WP3 Two-qubit gates and compatible stable qubits**  
D6 Assessment of experimental feasibility for existing qubit encodings and quantum gate schemes, M3.2, M3.5  
D7 Novel two-qubit gate schemes, M3.7
- **WP4 Generation and characterization of multi-particle entangled states**  
D8 Experimental generation of multi-particle entanglement in optical lattices, M4.1, M4.2, M4.3, M4.7  
D9 Measures and measurement procedures for multi-particle entanglement, M4.1
- **WP5 Strategies for minimizing decoherence**  
D11 Experimental realization of optical lattices with minimized decoherence  
M5.1, M5.3, M5.4, M5.5, M5.6

## *How to make a Superlattice II*



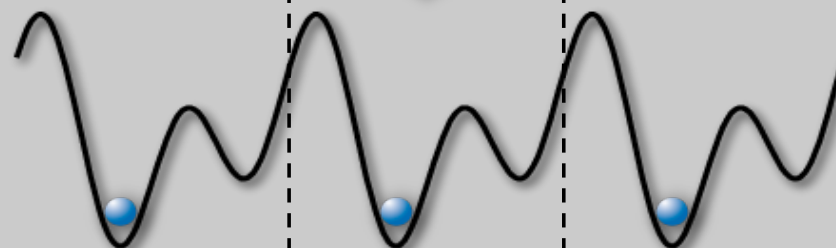
## *Patterned loading of the short lattice*



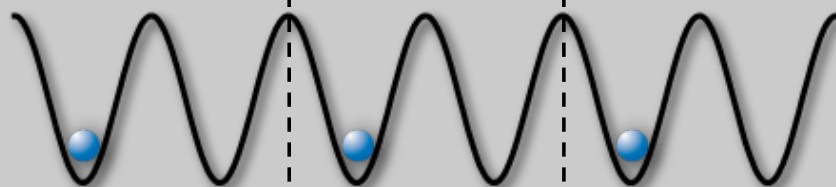
**Mott State in long lattice**



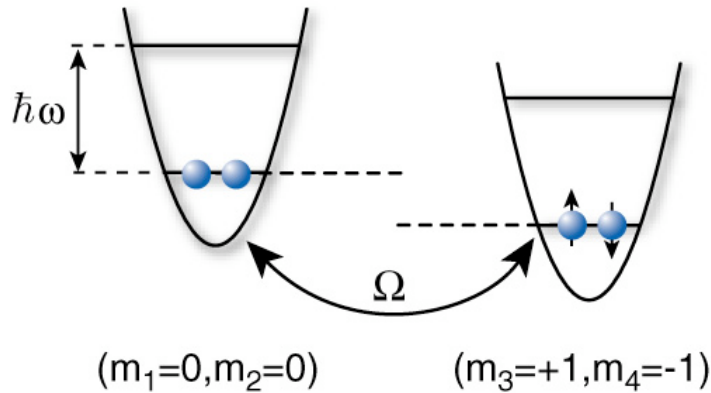
**Increase short lattice**



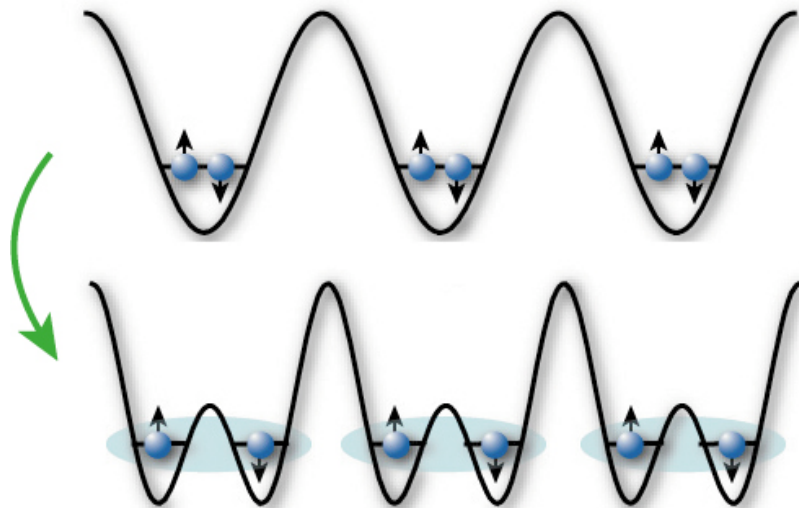
**Switch off long lattice**



# Robust multi-particle entanglement via spin changing collisions



A. Widera et al.,  
 Phys. Rev. Lett., 95,190405, (2005)



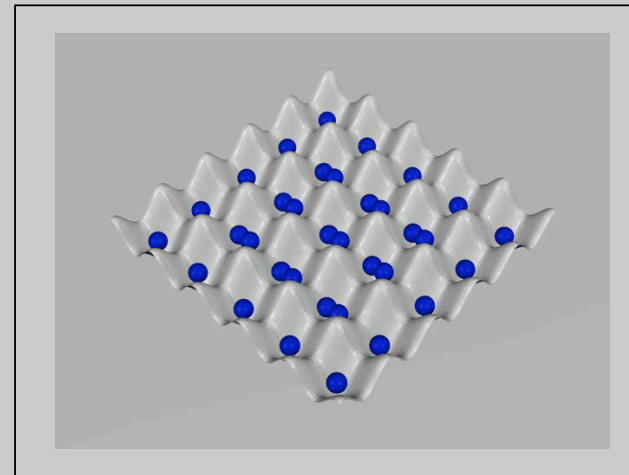
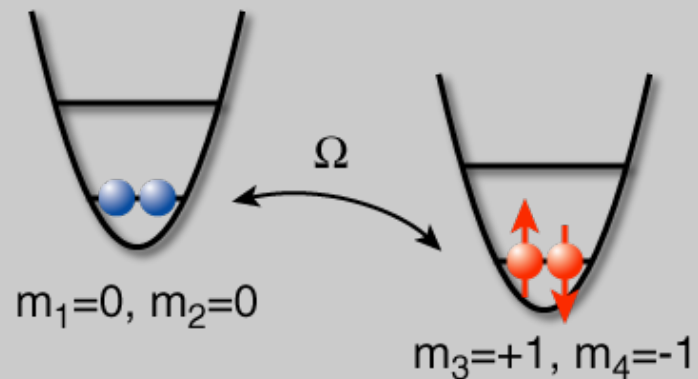
$$(|\uparrow, \downarrow\rangle + |\downarrow, \uparrow\rangle) \otimes |0, 0\rangle$$

**Spin Triplet**

$$|\uparrow\rangle_L |\downarrow\rangle_R + |\downarrow\rangle_L |\uparrow\rangle_R$$

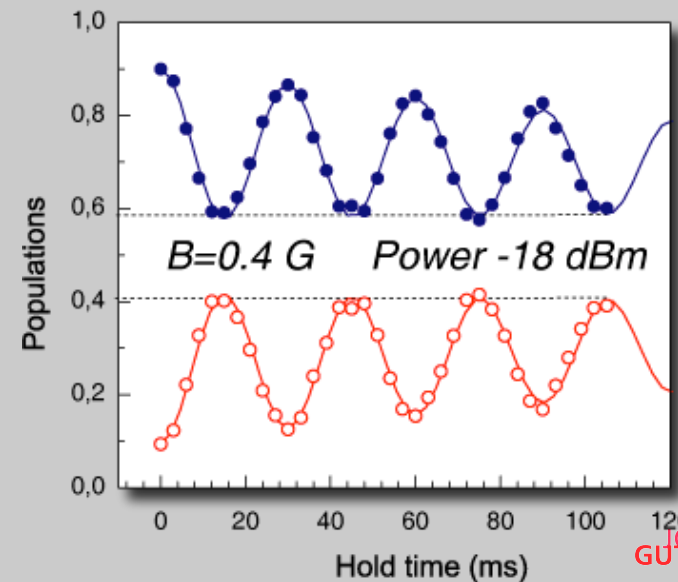
**Entangled Bell state**

# Spin Changing Collisions in an Optical Lattice



Collisionally induced  
„Rabi-Type“ Oscillations

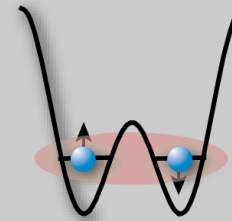
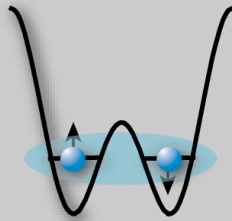
$$|0,0\rangle \leftrightarrow (|\uparrow,\downarrow\rangle + |\downarrow,\uparrow\rangle) / \sqrt{2}$$



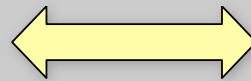
A. Widera et al., PRL 95, 190405 (2005)  
 Spinor dynamics without lattices:  
 Hamburg, GeorgiaTech, Berkley

## *Magnetic Gradient Fields Induce Singlet-Triplet Oscillations*

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$$|\uparrow\rangle_L |\downarrow\rangle_R + |\downarrow\rangle_L |\uparrow\rangle_R$$



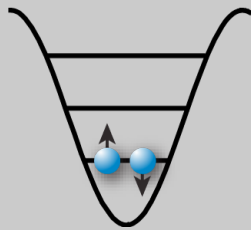
$$|\uparrow\rangle_L |\downarrow\rangle_R - |\downarrow\rangle_L |\uparrow\rangle_R$$

$$|\uparrow\rangle_L |\downarrow\rangle_R + e^{2i\phi(t)} |\downarrow\rangle_L |\uparrow\rangle_R$$

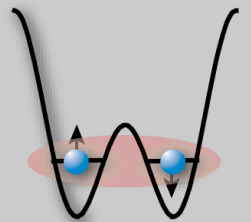
WP3 D6,7

$$\phi(t) = \mu_B B' d_{DW}$$

## How can we detect the Bell pairs? (2)

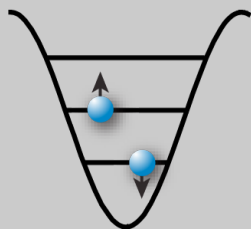


$$(|\uparrow, \downarrow\rangle + |\downarrow, \uparrow\rangle) \otimes |0, 0\rangle$$



Split

**When uniting bosonic spin singlet states, one particle has to occupy the excited band!**



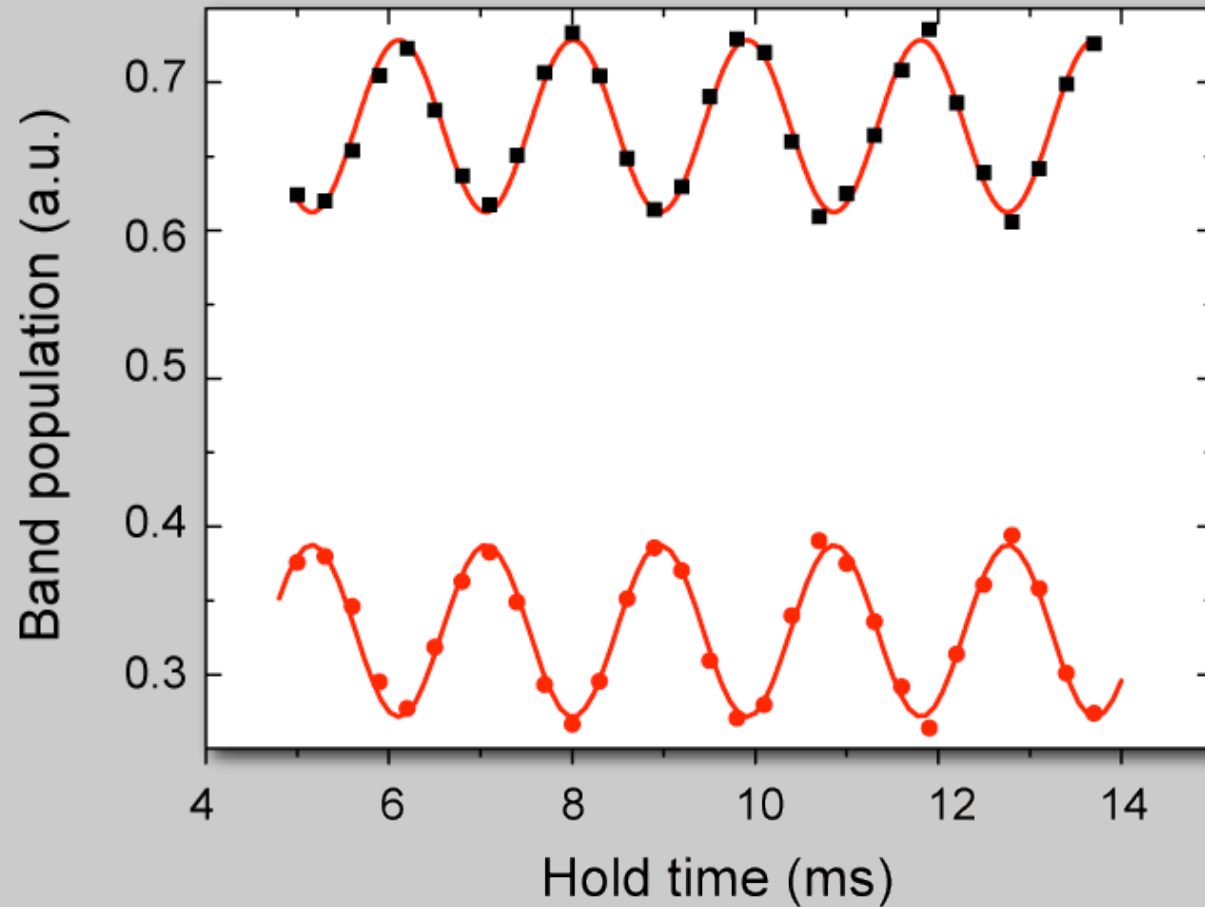
Unite

$$(|\uparrow, \downarrow\rangle + |\downarrow, \uparrow\rangle) \otimes (|0, 1\rangle + |1, 0\rangle)$$



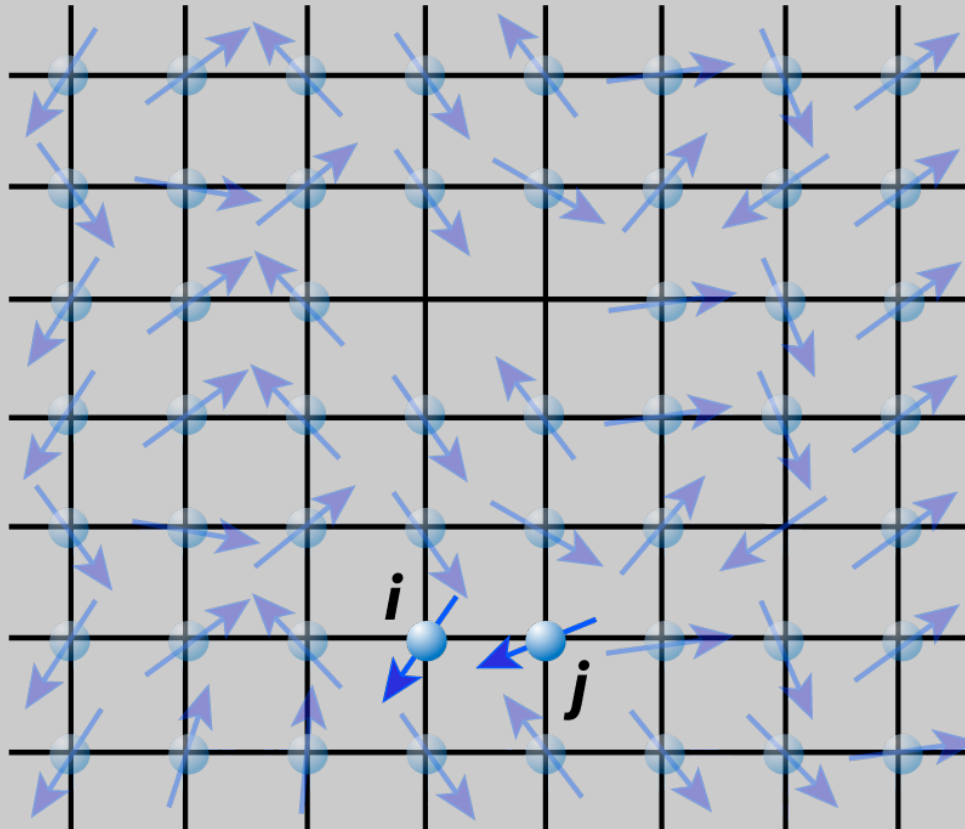
## *Singlet-Triplet Spin Oscillations*

**S. Trotzky** (in preparation)



See ion trap exps: C.F. Roos et al., PRL **92**, 220402 (2004),  
C. Langer et al., PRL **95**, 060502 (2005)

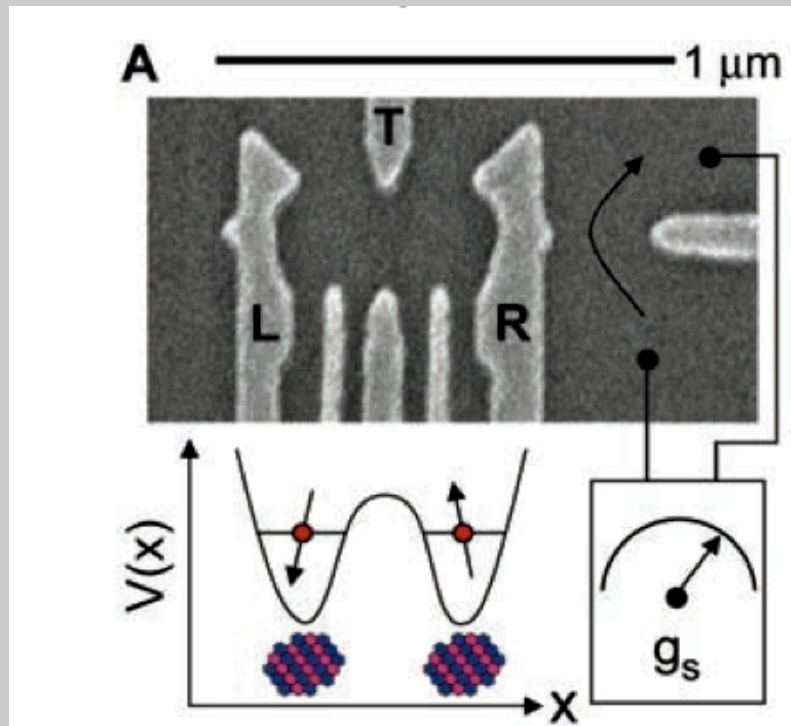
# Quantum Spin Systems in Optical Lattices



In strongly correlated electron system **spin-spin interactions** exist.

$$-J_{ex} \vec{S}_i \cdot \vec{S}_j$$

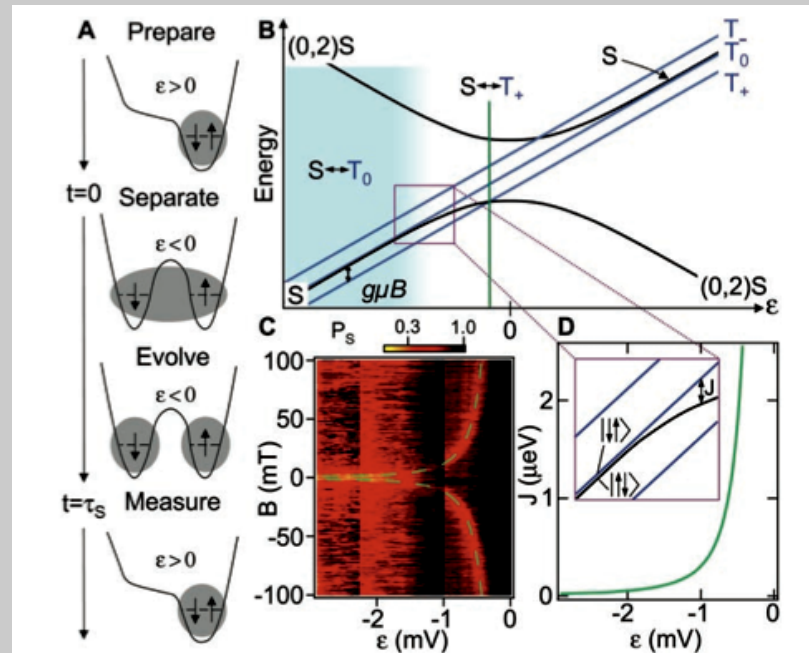
# Superexchange Coupling in Quantum Dots



Local control of spin states & interactions between spin states.

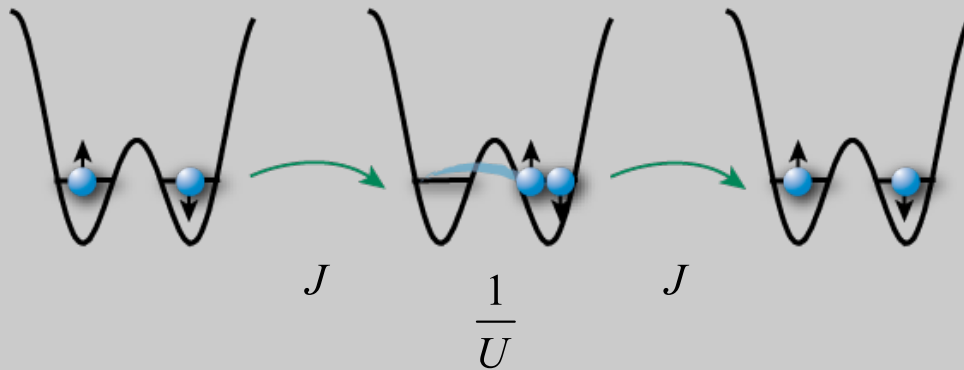
J.R. Petta et al., Science **309**, 2180 (2005)

## Coherent Manipulation of Coupled Electron Spins in Semiconductor Quantum Dots



# Quantum Magnetism

Second order hopping processes form the basis of **superexchange interactions!** (see e.g. A. Auerbach, Interacting Electrons and Quantum Magnetism)



$$-J \sum_{\langle i,j \rangle} \hat{a}_i^\dagger \hat{a}_j + \frac{1}{2} U \sum_i \hat{n}_i (\hat{n}_i - 1)$$

$$H = -J_{ex} \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j$$

$$J_{ex} \propto \frac{J^2}{U}$$

Ultracold atoms allow **tuning of Spin-Hamiltonians**

$$H = \sum_{\langle i,j \rangle} \left[ \lambda_{\mu z} \hat{\sigma}_i^z \hat{\sigma}_j^z \pm \lambda_{\mu \perp} (\hat{\sigma}_i^x \hat{\sigma}_j^x + \hat{\sigma}_i^y \hat{\sigma}_j^y) \right]$$

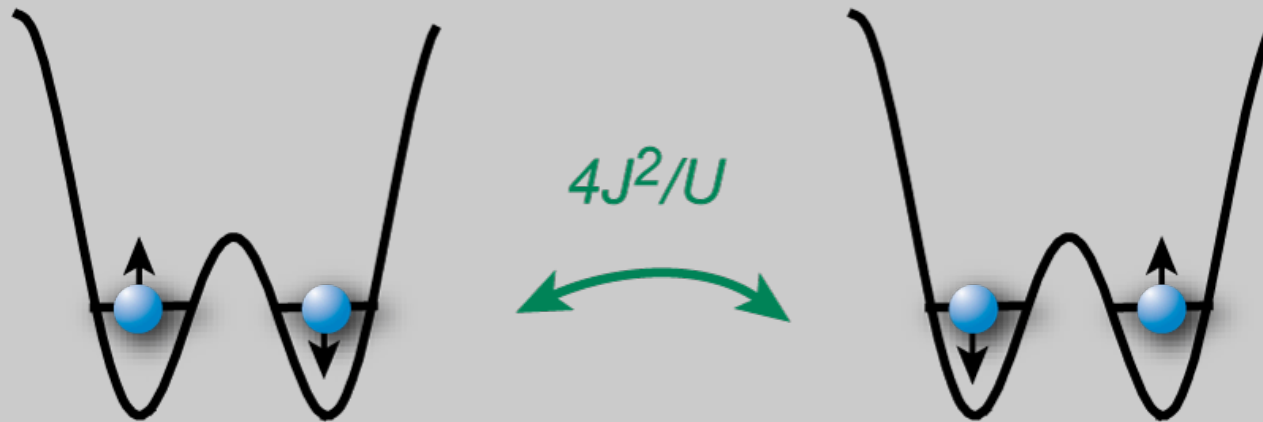
$$\lambda_{\mu z} = \frac{t_{\mu \uparrow}^2 + t_{\mu \downarrow}^2}{2U_{\uparrow \downarrow}} - \frac{t_{\mu \uparrow}^2}{U_{\uparrow}} - \frac{t_{\mu \downarrow}^2}{U_{\downarrow}}$$

$$\lambda_{\mu \perp} = \frac{t_{\mu \uparrow} t_{\mu \downarrow}}{U_{\uparrow \downarrow}}$$

L.M. Duan et al., PRL **91**, 090402 (2003),

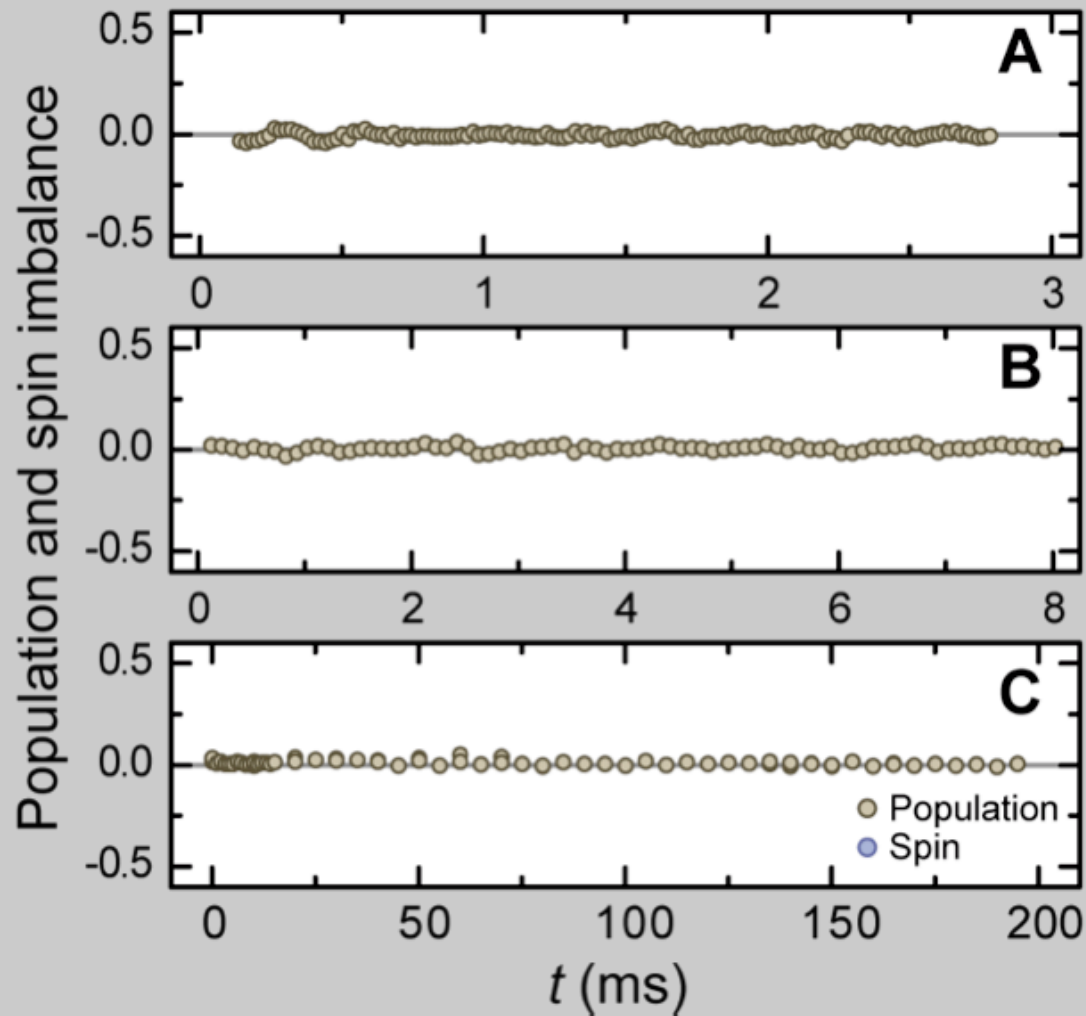
E. Altman et al., NJP **5**, 113 (2003), A.B. Kuklov et al. PRL **90**, 100401 (2003)

## *Superexchange induced flopping*



$$\begin{aligned} H_{\text{eff}} &= -J_{\text{ex}} \vec{S}_i \cdot \vec{S}_j \\ &= -\frac{J_{\text{ex}}}{2} (\hat{S}_i^+ \hat{S}_j^- + \hat{S}_i^- \hat{S}_j^+) - J_{\text{ex}} \hat{S}_i^z \hat{S}_j^z \end{aligned}$$

## Superexchange induced flopping



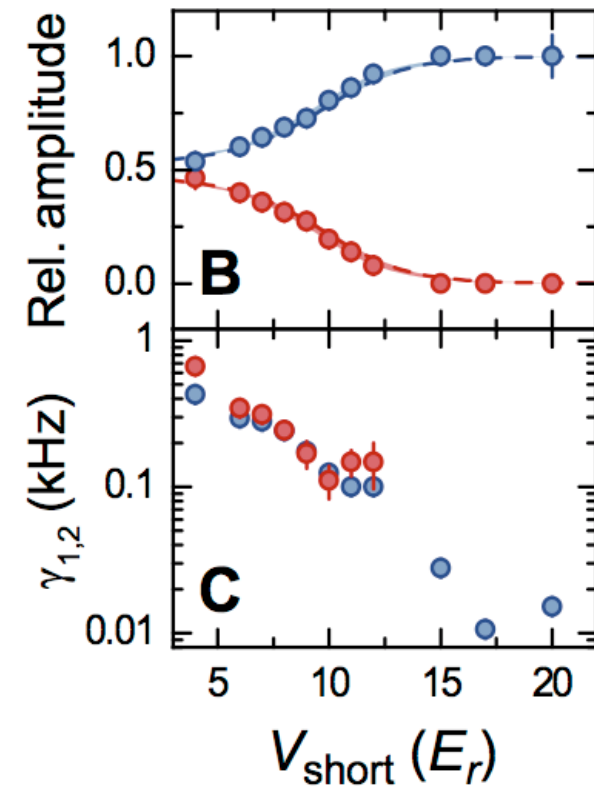
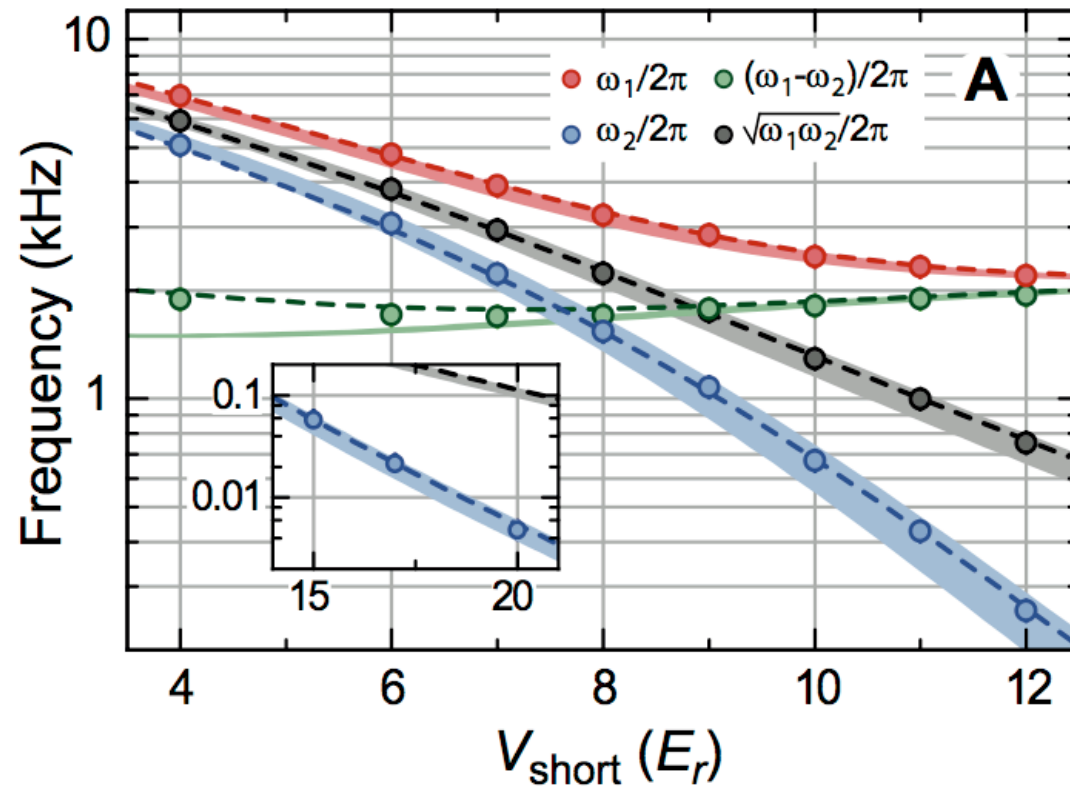
$$J/U = 1.25$$
$$V_{\text{short}} = 6 E_r$$

$$J/U = 0.26$$
$$V_{\text{short}} = 11 E_r$$

$$J/U = 0.05$$
$$V_{\text{short}} = 17 E_r$$

S. Trotzky et al. (*Science in press*)

## Measured Frequencies

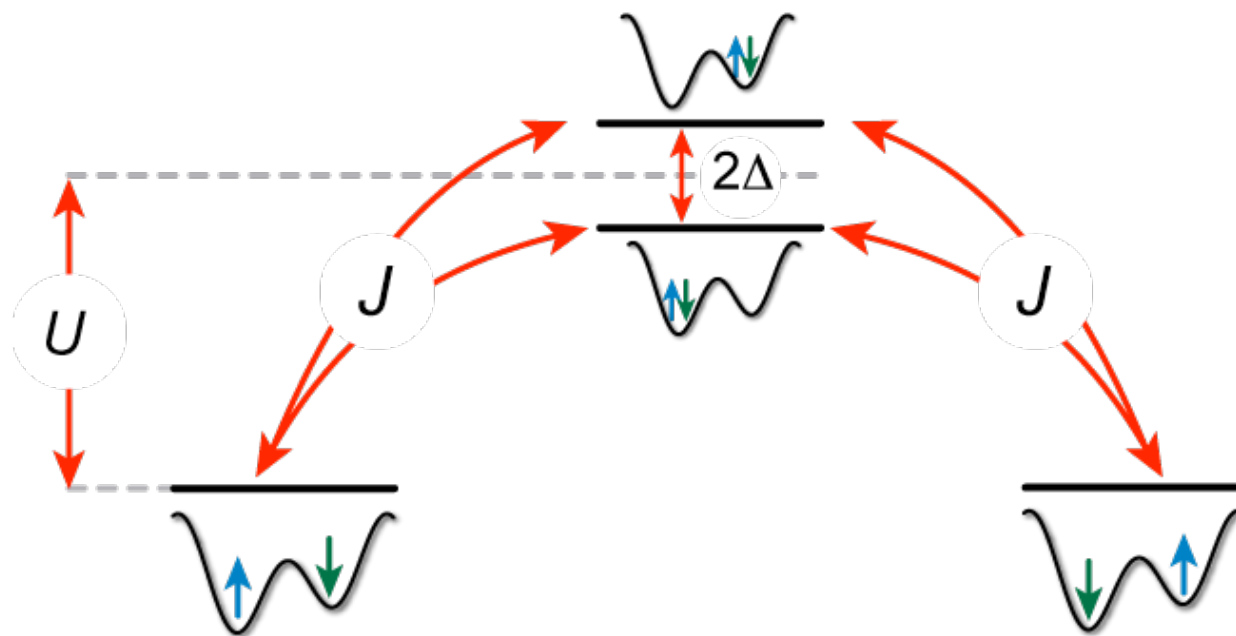


$$U' = U + 3U_{LR}$$

$$J'_{\text{ex}} = 2J'^2 / U - U_{LR}$$

## Controlling Superexchange Interactions

$$H_{eff} = -J_{ex} \vec{S}_i \cdot \vec{S}_j$$



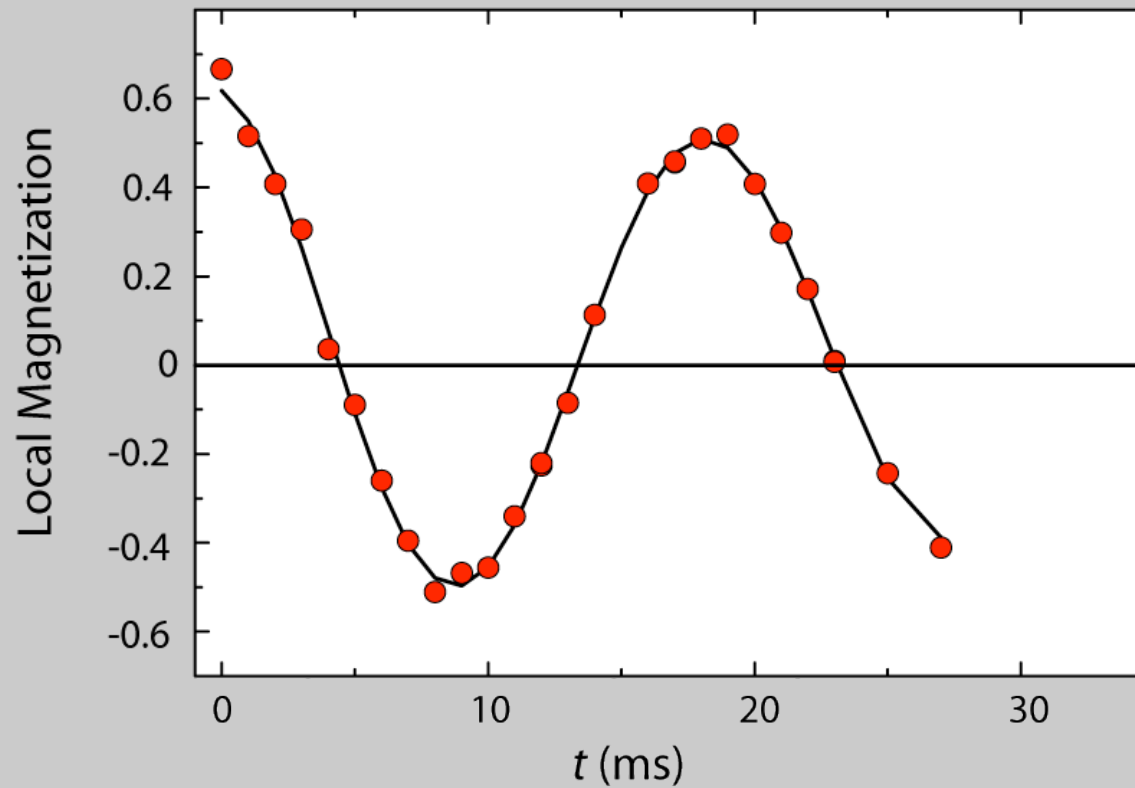
$$J_{ex} \propto \frac{J^2}{U + \Delta} + \frac{J^2}{U - \Delta}$$



## Controlling Superexchange Interactions

Time evolution under action of **ferromagnetic** superexchange

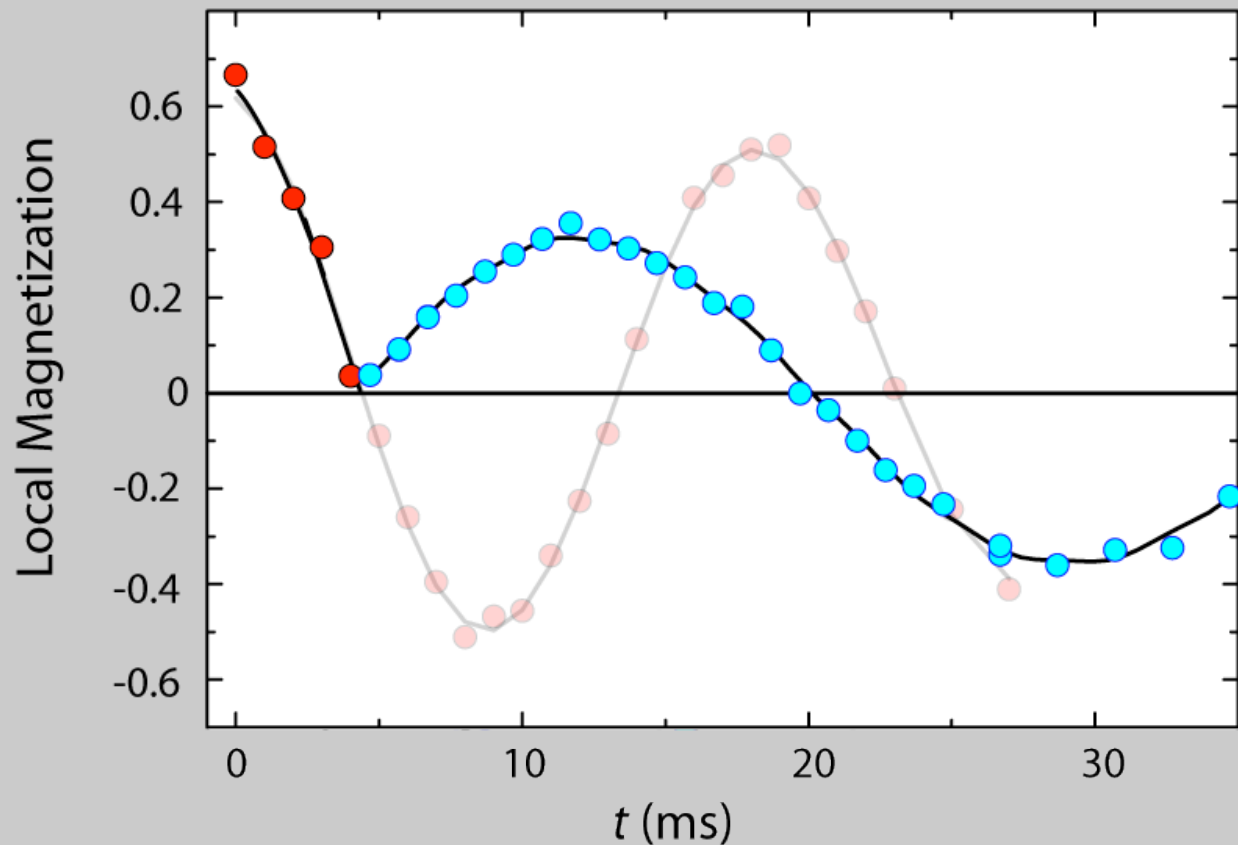
$$H_{eff} = -J_{ex} \vec{S}_i \cdot \vec{S}_j$$



## Controlling Superexchange Interactions

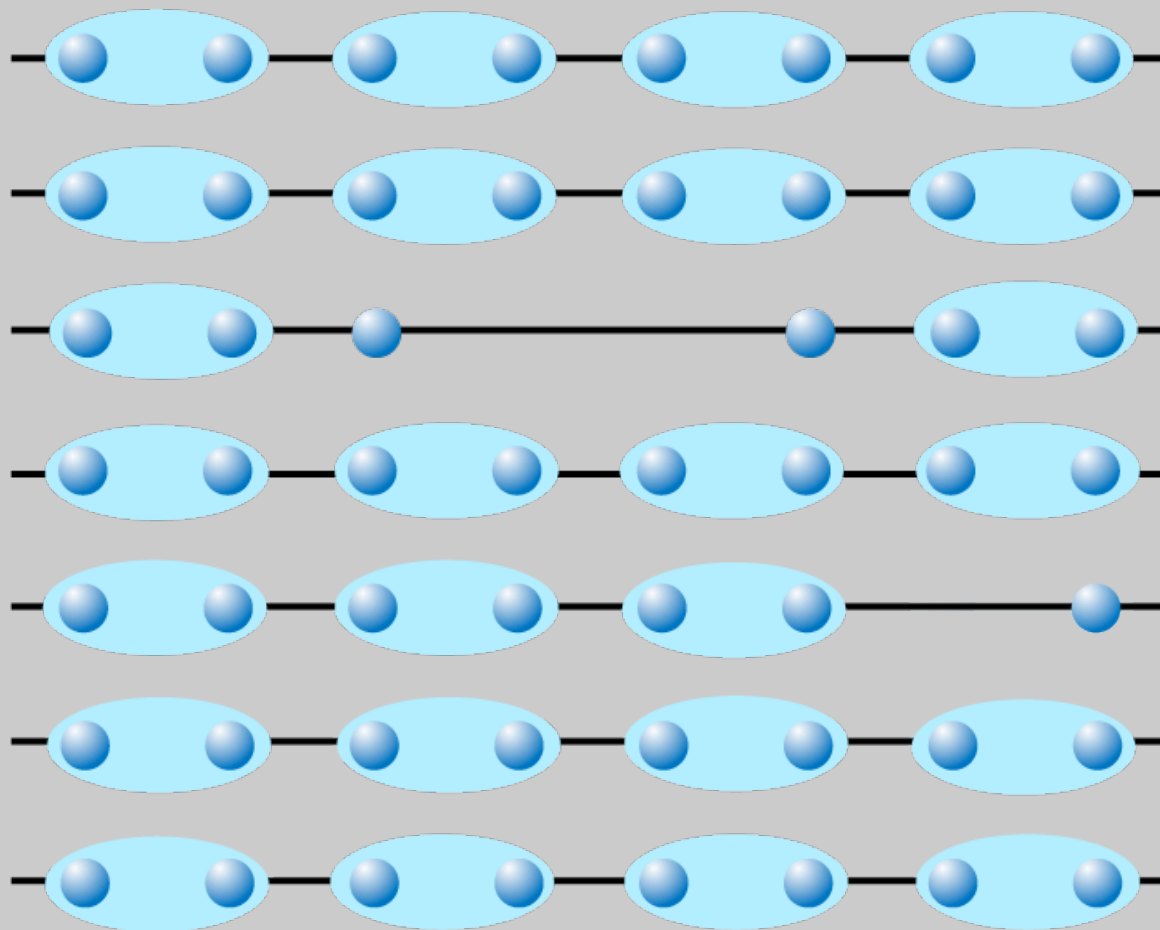
From **ferromagnetic** to **antiferromagnetic** superexchange interactions

$$H_{eff} = -J_{ex} \mathbf{S}_i \cdot \mathbf{S}_j \quad \longrightarrow \quad H_{eff} = +J'_{ex} \mathbf{S}_i \cdot \mathbf{S}_j$$



## *Arrays of Entangled Bell Pairs*

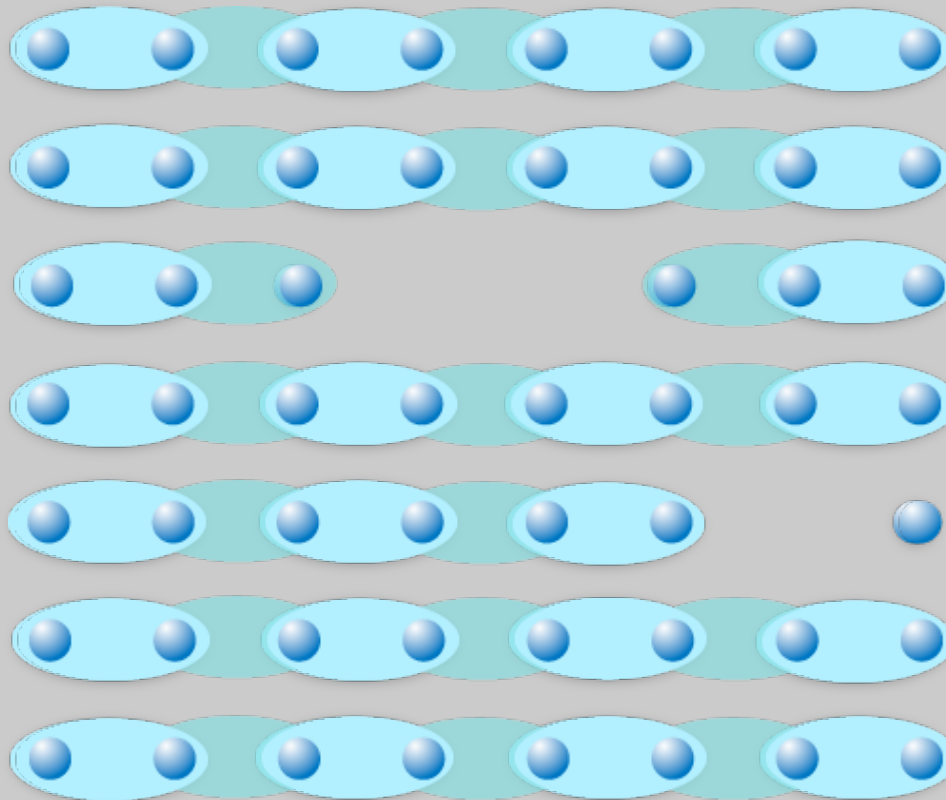
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A. M. Rey et al., PRL 99, 140601 (2007),  
B Vaucher, A Nunnenkamp and D. Jaksch, arXiv:0710:5099

## *Large Entangled States - Entanglement Knitting*

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**Pushbutton  
simultaneous  
creation of  
thousands of  
entangled Bell  
pairs in a single  
experiment.**

**Connection of  
entanglement possible  
via e.g. superexchange  
interactions.**

See also work of D. Jaksch et al.

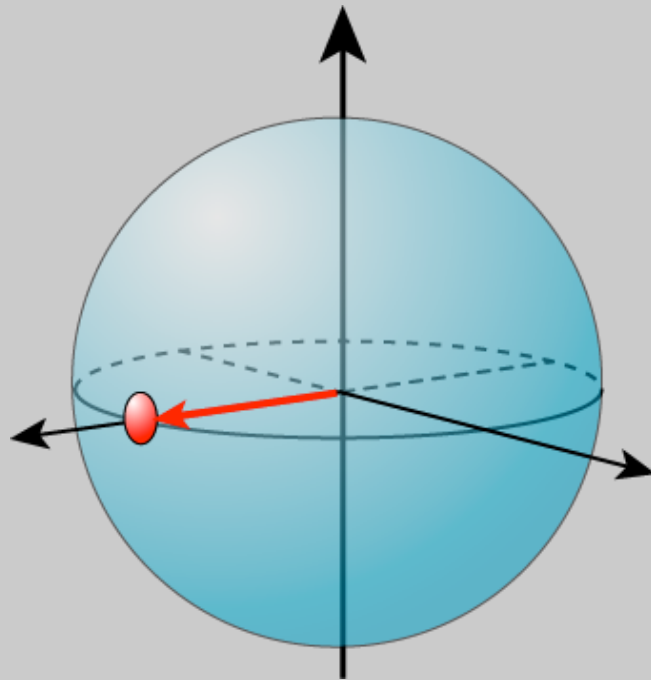


*Nonlinear Quantum Spin Dynamics in  
Bose-Einstein Condensates*

WP4

## *From Spin Squeezing to Schrödinger Cats - Nonlinear Quantum Spin Dynamics -*

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**What happens if you tune interactions in larger ensembles?**

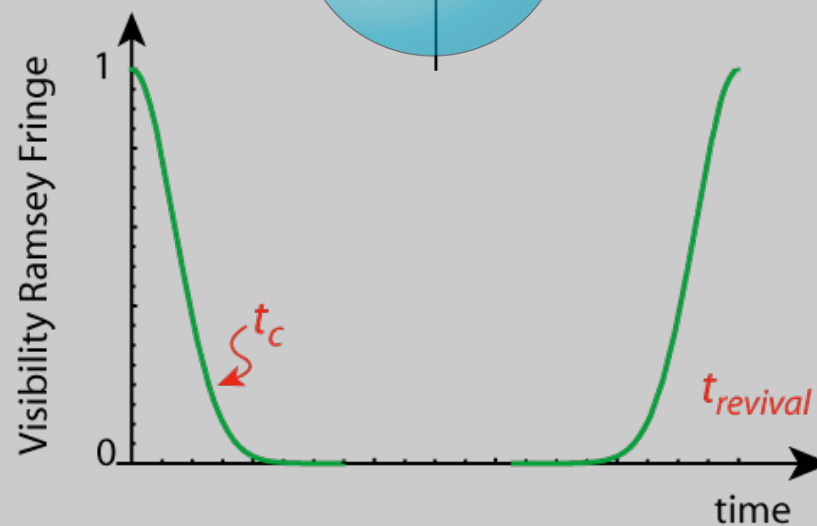
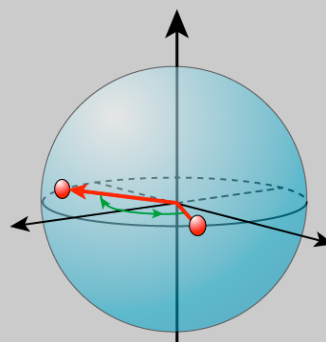
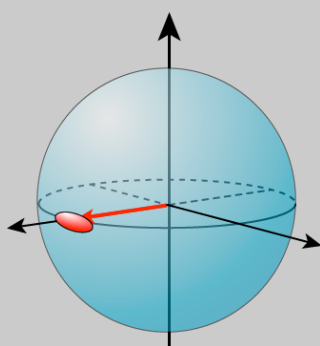
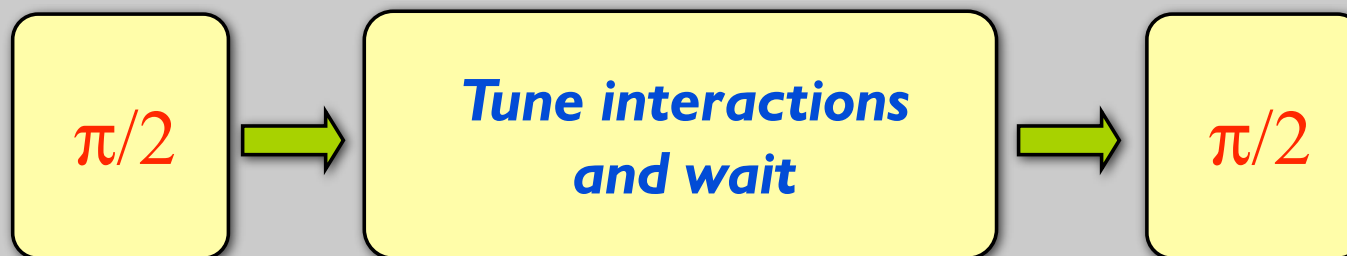
$$\left(\hat{a}^\dagger + \hat{b}^\dagger\right)^{\otimes N} |0\rangle$$

$$\hat{H} = \chi \hat{S}_z^2$$

$$\chi = a_{aa} + a_{bb} - 2a_{ab}$$

A. Sørensen et al., Nature 409, 63 (2001),  
L. You, PRA (2002),  
A. Micheli et al. PRA 67, 013607 (2003)

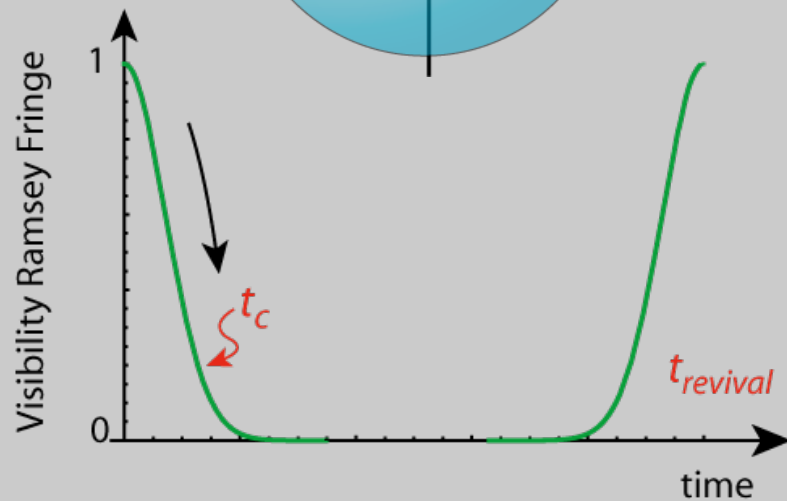
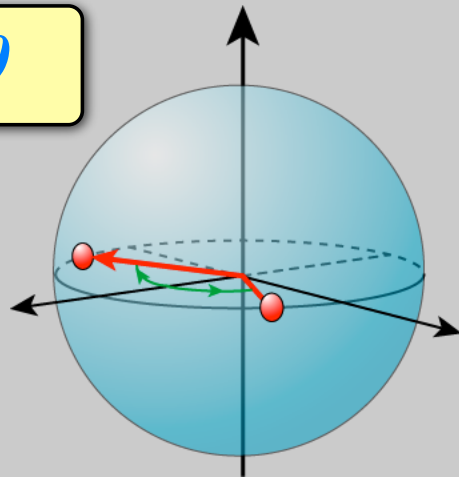
## Ramsey Fringe Visibility Evolution



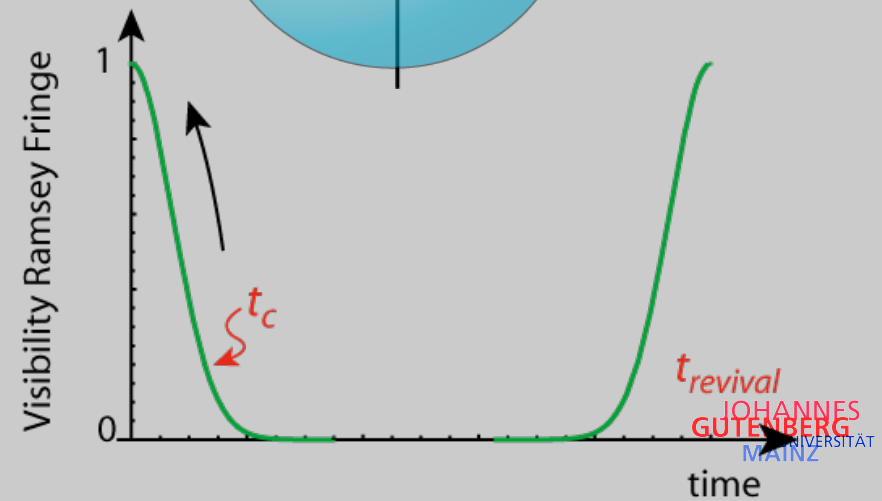
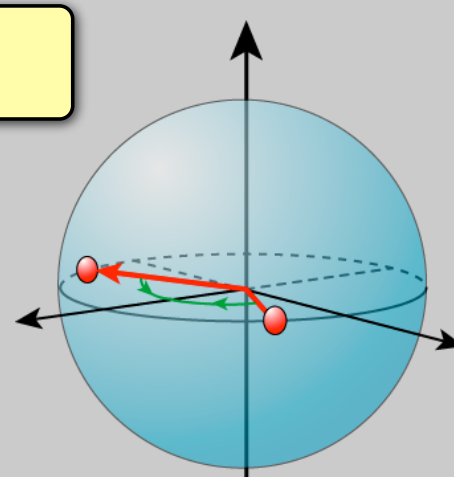
# Decoherence Problems

Full revival can so far not be reached due to decoherence, **but time evolution can be reversed!**

$$\chi < 0$$

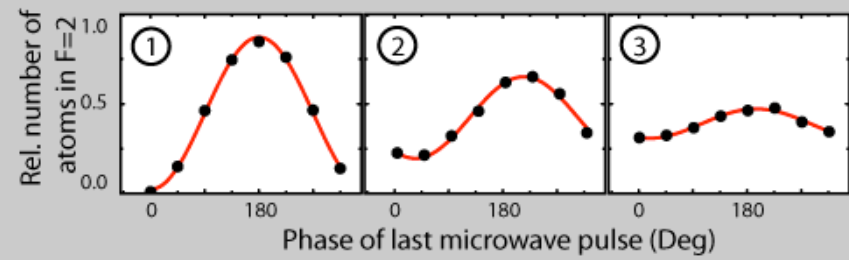
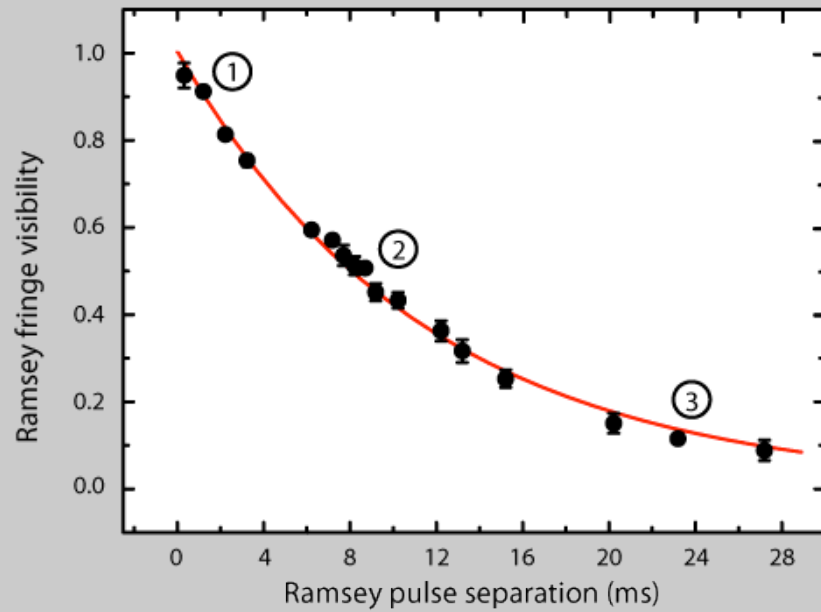


$$\chi > 0$$

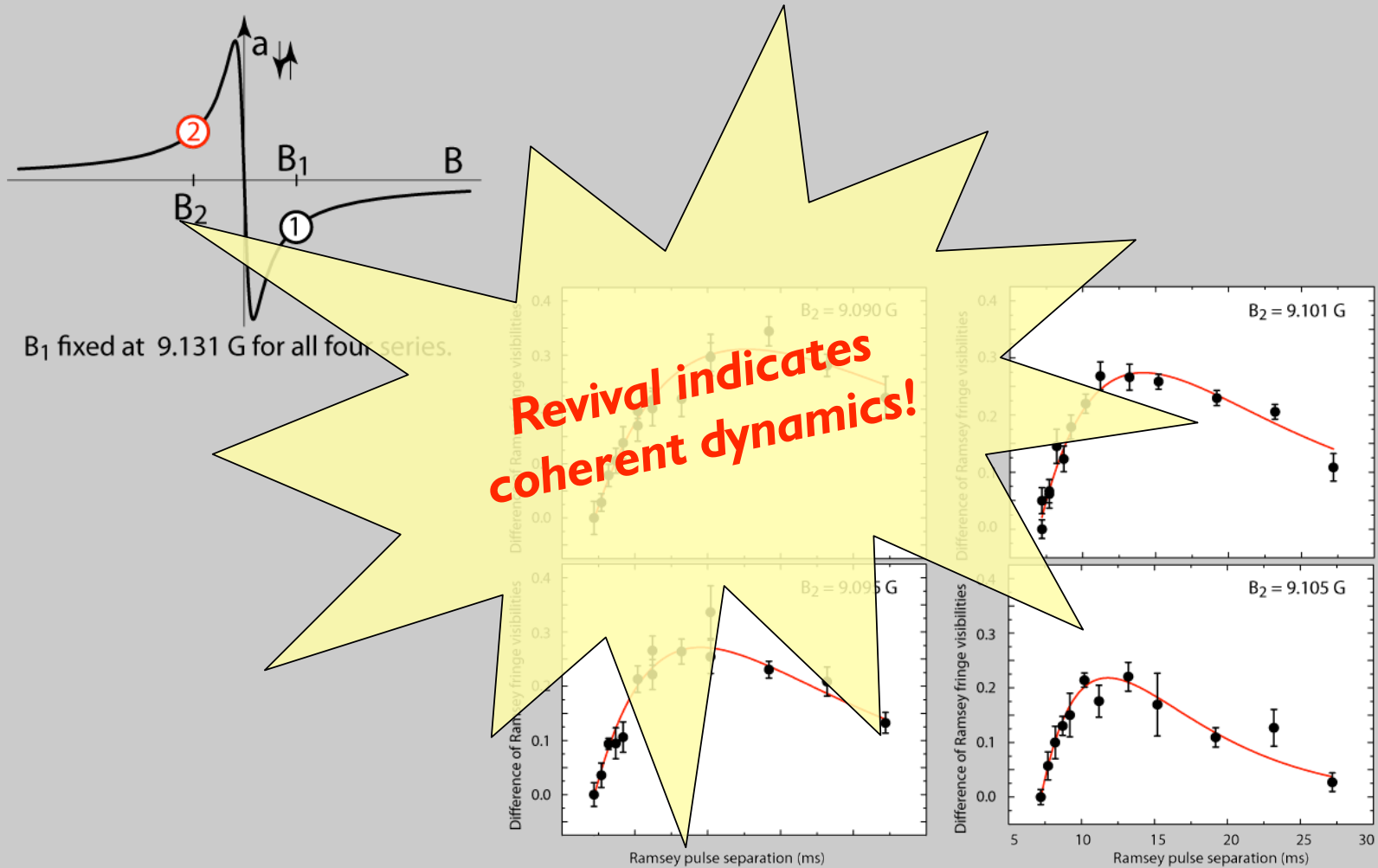




# Experimental Results



# Reversing the Coherent Dynamics



A. Widera et al.  
(submitted to PRL, arXiv:0709.2094)

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- **WP5 Strategies for minimizing decoherence**  
D11 Experimental realization of optical lattices with minimized decoherence  
M5.1, M5.3, M5.4, M5.5, M5.6

## Summary & Outlook



- Creation and loading of atoms in optical superlattices
- Single Qubit State Manipulation
- Massively Parallel Creation of Bell Pairs
- Characterization of Bell Pairs
- Measurement of Coherence Time of Single Qubits and Bell Pairs
- Controllable Superexchange Spin-Spin Interaction
- Novel Multiparticle Entanglement Schemes for Generation of Robust MP Entangled Quantum States
- Multiparticle Entanglement via Spin-Squeezing in 1D Quantum Systems
- Investigation of Dynamical Effects in Mode-Squeezed 1D Luttinger Liquids

- How defect free can we create array of Bell pairs?  
Can we observe dynamical effects of quantum spin systems and compare to advanced numerical methods?
- How longlived can multiparticle states be with zero magnetization?
- Can we create/engineer **topologically ordered quantum states** and use them for topological quantum computation?



FP6-2002-IST-C